

Princeton University  
COS 217: Introduction to Programming Systems  
Fall 2007 Final Exam Answers

The exam was a three-hour, open-book, open-notes exam.

**Question 1 Part 1**

10101010  
SEEEEMMM

$$\begin{aligned} N &= (-1)^S * 1.M * 2^{E-7} \\ &= (-1)^1 * 1.010 * 2^{5-7} \\ &= -1 * 1.010 * 2^{-2} \\ &= -1 * 101 * 2^{-4} \\ &= -5/16 \end{aligned}$$

**Question 1 Part 2**

10000010  
SEEEEMMM

$$\begin{aligned} N &= (-1)^S * 0.M * 2^{-7+1} \\ &= (-1)^1 * 0.010 * 2^{-6} \\ &= -1 * 0.010 * 2^{-6} \\ &= -1 * 1 * 2^{-8} \\ &= -1/256 \end{aligned}$$

**Question 1 Part 3**

$$\begin{aligned} N &= (-1)^S * 0.M * 2^{-(2^{10-1}) + 1} \\ &= (-1)^S * 0.M * 2^{-(1024-1) + 1} \\ &= (-1)^S * 0.M * 2^{-1023 + 1} \\ &= (-1)^S * 0.M * 2^{-1022} \end{aligned}$$

**Question 1 Part 4**

$$\begin{aligned} N &= (-1)^S * 1.M * 2^{E-(2^{10-1})} \\ N &= (-1)^S * 1.M * 2^{E-(1024-1)} \\ N &= (-1)^S * 1.M * 2^{E-1023} \end{aligned}$$

## Question 2 Part 1

3

## Question 2 Part 2

```
-----  
fib(1) temp 0  
      n    1  
-----  
fib(2) temp 0  
      n    2  
-----  
fib(3) temp 0  
      n    3  
-----
```

Alternate answer:

```
-----  
fib(0) temp 0  
      n    0  
-----  
fib(2) temp 1  
      n    2  
-----  
fib(3) temp 0  
      n    3  
-----
```

## Question 3 Part 1

Given: There are  $2^{32}$  addressable bytes.

Given: There are  $2^{12}$  bytes per page.

So there are  $2^{20}$  addressable pages, and there must be  $2^{20}$  entries in a process's page table.

Given: Each page table entry is 32 bits (alias 4 bytes) long.

So a process's page table consumes  $2^{20}$  entries \* 4 bytes per entry =  $2^{22}$  bytes.

## Question 3 Part 2

1 GB =  $2^{30}$  bytes.  $2^{22}/2^{30} = 1/2^8 = 1/256$ . So each page table would consume 1/256 of physical memory.

So as long as the number of processes is substantially below 256, the virtual memory scheme is practical on a laptop with 1 GB of physical memory installed.

## Question 3 Part 3

Given: There are  $2^{64}$  addressable bytes.

Given: There are  $2^{12}$  bytes per page.

So there are  $2^{52}$  addressable pages, and there must be  $2^{52}$  entries in a process's page table.

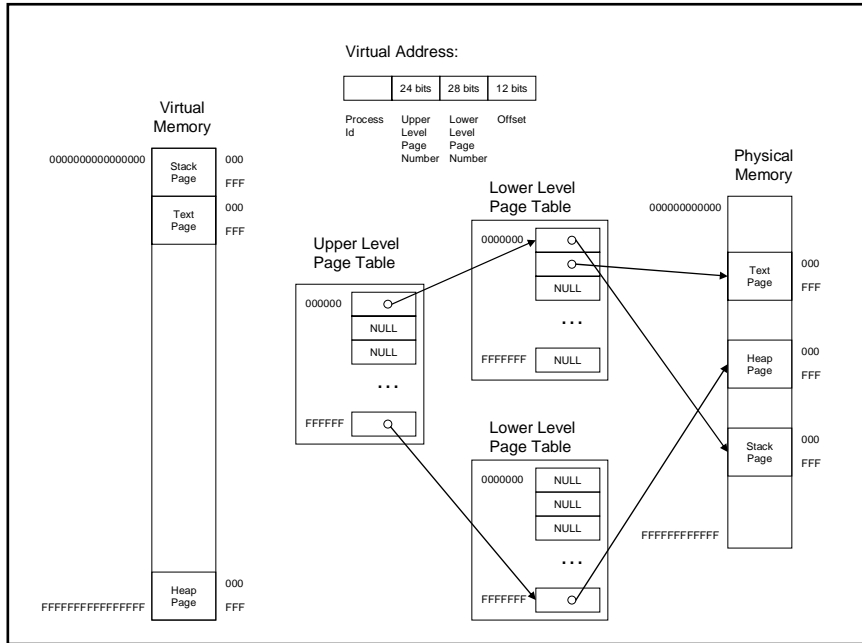
Given: Each page table entry is 48 bits (alias 6 bytes) long.

So a process's page table consumes  $2^{52}$  entries \* 6 bytes per entry =  $2^{52} * 2 * 3$  bytes =  $3 * 2^{53}$  bytes.

### Question 3 Part 4

8 GB =  $8 * 2^{30}$  bytes =  $2^{33}$  bytes.  $2^{33}$  bytes is much less than  $3 * 2^{53}$  bytes. So the page table for a single process would not fit in all of physical memory. So the virtual memory scheme is impractical on a server with 8 GB of physical memory installed.

### Question 3 Part 5



### Question 4

This is the DFA in textual form:

```

START_STATE (S)
  H: H_STATE
  D: D_STATE
  other: START_STATE

H_STATE
  u: Hu_STATE
  H: H_STATE
  D: D_STATE
  other: START_STATE

Hu_STATE
  m: Hum_STATE
  H: H_STATE
  D: D_STATE
  other: START_STATE

Hum_STATE
  p: Hump_STATE
  H: H_STATE
  D: D_STATE
  other: START_STATE

Hump_STATE
  t: HumpT_STATE
  H: H_STATE
  D: D_STATE
  
```

```

other: START_STATE

Humpt_STATE
y: Humpty_STATE
H: H_STATE
D: D_STATE
other: START_STATE

Humpty_STATE
D: HumptyD_STATE
other: Humpty_STATE

HumptyD_STATE
u: HumptyDu_STATE
D: HumptyD_STATE
other: Humpty_STATE

HumptyDu_STATE
m: HumptyDum_STATE
D: HumptyD_STATE
other: Humpty_STATE

HumptyDum_STATE
p: HumptyDump_STATE
D: HumptyD_STATE
other: Humpty_STATE

HumptyDump_STATE
t: HumptyDumt_STATE
D: HumptyD_STATE
other: Humpty_STATE

HumptyDumt_STATE
y: SUCCESS_STATE
D: HumptyD_STATE
other: Humpty_STATE

D_STATE
u: Du_STATE
D: D_STATE
H: H_STATE
other: START_STATE

Du_STATE
m: Dum_STATE
D: D_STATE
H: H_STATE
other: START_STATE

Dum_STATE
p: Dump_STATE
D: D_STATE
H: H_STATE
other: START_STATE

Dump_STATE
t: Dumt_STATE
D: D_STATE
H: H_STATE
other: START_STATE

Dumt_STATE
y: Dumpty_STATE
D: D_STATE
H: H_STATE
other: START_STATE

Dumpty_STATE
H: DumptyH_STATE
other: Dumpty_STATE

```

```
DumptyH_STATE
u: DumptyHu_STATE
H: DumptyH_STATE
other: Dumpty_STATE
```

```
DumptyHu_STATE
m: DumptyHum_STATE
H: DumptyH_STATE
other: Dumpty_STATE
```

```
DumptyHum_STATE
p: DumptyHump_STATE
H: DumptyH_STATE
other: Dumpty_STATE
```

```
DumptyHump_STATE
t: DumptyHumpt_STATE
H: DumptyH_STATE
other: Dumpty_STATE
```

```
DumptyHumpt_STATE
y: SUCCESS_STATE
H: DumptyH_STATE
other: Dumpty_STATE
```

```
SUCCESS_STATE (F)
all: SUCCESS_STATE
```

### **Question 5 Part 1**

In line 1, ".roadata" should be ".rodata".

### **Question 5 Part 2**

The loop within the convert\_byte() function prints the least significant binary digit, followed by the next least significant binary digit, etc. It should print the most significant binary digit, followed by the next most significant binary digit, etc.

### **Question 5 Part 3**

The main() function is missing its epilog. That is, the main() function fails to restore the values of the EBP and ESP registers, and fails to pop the old value of EBP from the stack. Thus, when the ret instruction executes, the item at the top of the stack is not the return address. So flow of control returns to an improper place in memory.

### **Question 5 Part 4**

```
.section ".rodata"
cFormat1:
    .asciz "%d"
    .align 4
cFormat2:
    .string "Enter a number between 0 and 255: "

    .section ".text"
## Formal parameter offset
    .equ BYTE, 8

## Local variable offset
    .equ COUNT, -4

## Constants
    .equ INITIAL_COUNT, 8
    .equ MASK, 0x80
    .globl convert_byte
    .type convert_byte, @function
convert_byte:
    pushl %ebp
    movl %esp, %ebp
```

```

    pushl %ebx
    pushl %esi
    movl $INITIAL_COUNT, %esi
    movl BYTE(%ebp), %eax
    movl %eax, %ebx
    jmp .L2

.L3:
    movsx %bl, %eax
    andl $MASK, %eax
    shr1 $7, %eax
    movl %eax, 4(%esp)
    movl $cFormat1, (%esp)
    call printf
    movsx %bl, %eax
    sall %eax
    movl %eax, %ebx

.L2:
    subl $1, %esi
    cmpl $-1, %esi
    jne .L3
    movl $10, (%esp)
    call putchar
    popl %esi
    popl %ebx
    movl %ebp, %esp
    popl %ebp
    ret

## Local variable offset
.equ MAINBYTE, -5
.equ NUM, -8

## Constants
.equ INITIAL_COUNT, 8

.globl main
.type main, @function
main:
    pushl %ebp
    movl %esp, %ebp
    subl $8, %esp
    movl $cFormat2, (%esp)
    call printf
    leal NUM(%ebp), %eax
    movl %eax, 4(%esp)
    movl $cFormat1, (%esp)
    call scanf
    movl NUM(%ebp), %eax
    movb %al, MAINBYTE(%ebp)
    movsx MAINBYTE(%ebp), %eax
    movl %eax, (%esp)
    call convert_byte
    movl $0, %eax
    addl $8, %esp
    movl %ebp, %esp
    popl %ebp
    ret

```

## Question 5 Part 5

The movsx (move with sign extension) instruction copies the contents of the source operand to the destination operand, and sign extends the value throughout the destination operand.

## Question 5 Part 6

```
.section ".rodata"
cFormat1:
    .asciz "%d"
    .align 4
cFormat2:
    .string "Enter a number between 0 and 4294967295: "

    .section ".text"
## Formal parameter offset
    .equ BYTE, 8

## Local variable offset
    .equ COUNT, -4

## Constants
    .equ INITIAL_COUNT, 32
    .equ MASK, 0x80000000
    .globl convert_byte
    .type convert_byte, @function
convert_byte:
    pushl %ebp
    movl %esp, %ebp
    pushl %ebx
    pushl %esi
    movl $INITIAL_COUNT, %esi
    movl BYTE(%ebp), %eax
    movl %eax, %ebx
    jmp .L2

.L3:
    movl %ebx, %eax
    andl $MASK, %eax
    shr1 $31, %eax
    movl %eax, 4(%esp)
    movl $cFormat1, (%esp)
    call printf
    movl %ebx, %eax
    sall %eax
    movl %eax, %ebx

.L2:
    subl $1, %esi
    cmpl $-1, %esi
    jne .L3
    movl $10, (%esp)
    call putchar
    popl %esi
    popl %ebx
    movl %ebp, %esp
    popl %ebp
    ret

## Local variable offset
    .equ MAINBYTE, -8
    .equ NUM, -8

## Constants
    .equ INITIAL_COUNT, 8

    .globl main
    .type main, @function
main:
    pushl %ebp
    movl %esp, %ebp
    subl $8, %esp
    movl $cFormat2, (%esp)
    call printf
```

```

    leal NUM(%ebp), %eax
    movl %eax, 4(%esp)
    movl $cFormat1, (%esp)
    call scanf
    movl NUM(%ebp), %eax
    # Deleted two lines from this place.
    movl %eax, (%esp)
    call convert_byte
    movl $0, %eax
    addl $8, %esp
    movl %ebp, %esp
    popl %ebp
    ret

```

## Question 6

The answers to Question 6 Part1 and Part 2 were provided by Lindsey Poole.

The following are example solutions. Your solution will differ.

For full marks, your solution should:

- Not rely on operational precedence.
- Not assume ASCII.
- Not assume data type sizes.
- Remove magic numbers.
- Not use gets().
- Use assert() for function parameters and memory allocations.
- Free allocated memory

We accepted other solutions that ameliorated these problems.

### Question 6 Part 1

```

#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
#include <ctype.h>

void invertCase(int *buf, int *numChar)
{
    int i;

    /* Don't rely on operational precedence. */
    for(i = 0; i < 1024; i++) {
        /* don't assume ascii */
        if (isupper(buf[i])) {
            buf[i] = tolower(buf[i]);
        } else if (islower(buf[i])) {
            buf[i] = toupper(buf[i]);
        }
    }

    *numChar = i;
}

void getData(int *buf)
{
    /* Don't use gets(). Need to use
    * getc() since buf is int now. */
    int i;
    for (i=0; i < 1024; i++) {
        buf[i] = getc(stdin);
        if (buf[i] == EOF || buf[i] == '\n')
            break;
    }
    buf[i + 1] = 0;
}

void writeData(int *buf)
{

```



```

    int i;
    /* Must use putc() since buf is int now. */
    for (i=0; i < 1024; i++) {
        putc(buf[i], stdout);
        if (buf[i] == 0)
            break;
    }
}

int main(int argc, char *argv[])
{
    int *buf;
    int *numChar;

    /* Don't assume data type sizes.
     * buf is int for internationalization. */
    buf = calloc(1024, sizeof(int));
    numChar = calloc(1, sizeof(int));

    getData(buf);
    invertCase(buf, numChar);
    writeData(buf);

    return 0;
}

```

## **Question 6 Part 2**

```

#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
#include <ctype.h>

/* Define MAX_LEN. */
enum {MAX_LEN = 1024};

void invertCase(int *buf, int *numChar)
{
    int i;
    /* Assert buf != NULL. */
    /* Assert numChar != NULL. */
    assert(buf != NULL);
    assert(numChar != NULL);

    /* Use MAX_LEN and null terminator*/
    for(i = 0; i < MAX_LEN && buf[i] != 0; i++) {
        /* don't assume ascii */
        if (isupper(buf[i])) {
            buf[i] = tolower(buf[i]);
            /* Make numchar useful. */
            (*numChar)++;
        } else if (islower(buf[i])) {
            buf[i] = toupper(buf[i]);
            /* Make numchar useful. */
            (*numChar)++;
        }
    }
}

void getData(int *buf)
{
    int i;
    /* Assert buf != NULL. */
    assert(buf != NULL);

    /* Use MAX_LEN. */
    for (i=0; i < MAX_LEN-1; i++) {
        buf[i] = getc(stdin);
        if (buf[i] == EOF || buf[i] == '\n')

```

```

        break;
    }
    buf[i + 1] = 0;
}

void writeData(int *buf, int *numChar)
{
    int i;
    /* Assert buf != NULL. */
    /* Assert numChar != NULL. */
    assert(buf != NULL);
    assert(numChar != NULL);

    /* Use MAX_LEN. */
    for (i=0; i < MAX_LEN; i++) {
        putchar(buf[i], stdout);
        if (buf[i] == 0)
            break;
    }

    /* Make numChar do something useful. */
    printf("%d characters converted\n", *numChar);
}

int main(int argc, char *argv[])
{
    int *buf;
    int *numChar;

    /* Use MAX_LEN. */
    buf = calloc(MAX_LEN, sizeof(int));
    numChar = calloc(1, sizeof(int));

    /* Assert buf != NULL. */
    /* Assert numChar != NULL. */
    assert(buf != NULL);
    assert(numChar != NULL);

    getData(buf);
    invertCase(buf, numChar);
    writeData(buf, numChar);

    /* Free buf. */
    /* Free numChar. */
    free(buf);
    free(numChar);

    return 0;
}

```

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